

CHAPTER FIVE

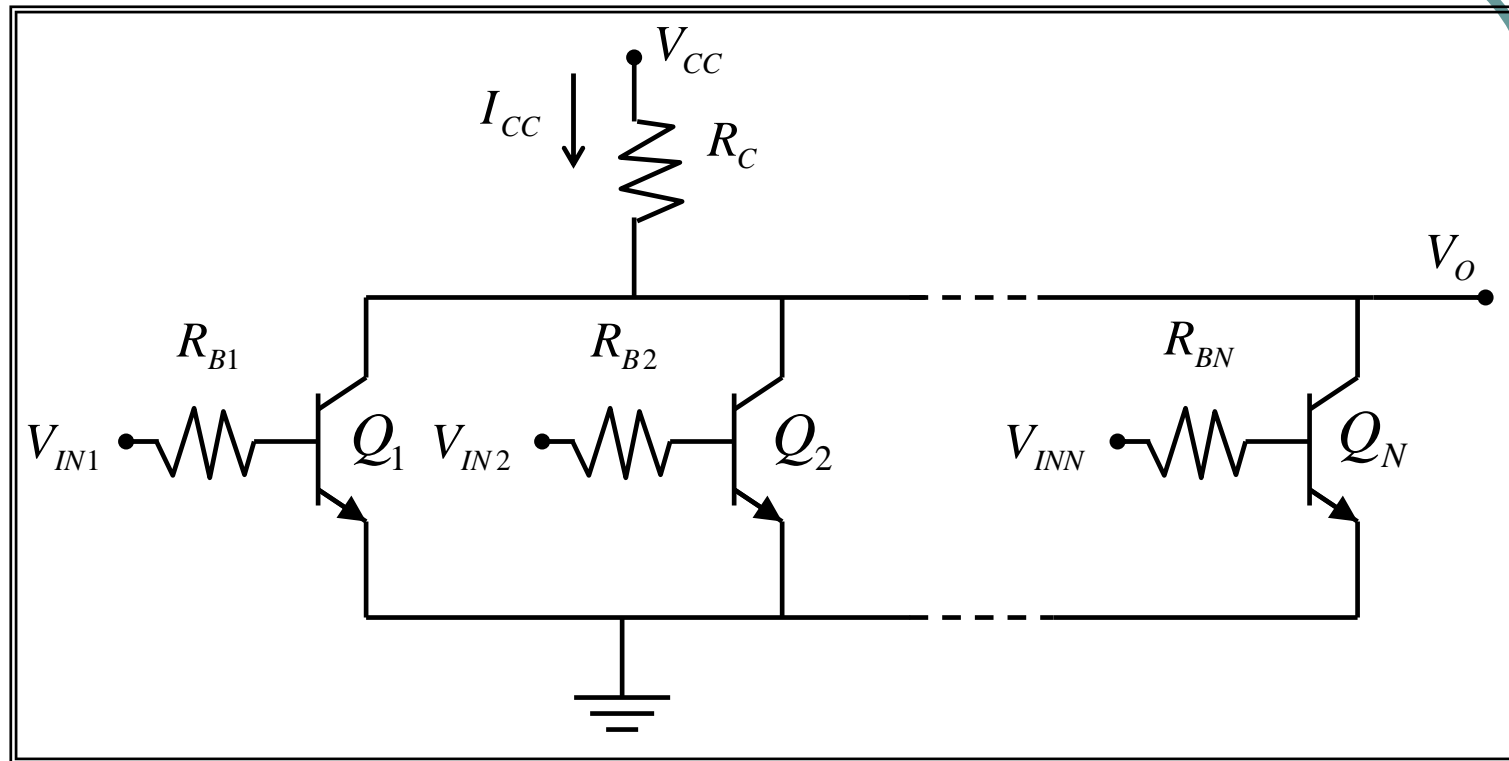
RTL NOR Gate

Digital Electronics.

Introduction

- RTL Inverter: discussed in Ch.4 ✓
- RTL NOR gate
- RTL NAND gate
- RTL OR gate
- RTL AND gate

Basic RTL NOR Gate



$$I_{CC} = \sum_{n=1}^N I_{Cn}$$

$$V_O = V_{CC} - I_{CC} R_C$$

If all inputs are less than V_{BE} (FA)



$$V_O = V_{CC}$$

High

If at least one input is greater than V_{IH}



$$V_O = V_{CE} (sat)$$

Low

Basic RTL NAND Gate

Assuming $\beta_F \gg 1$, I_B is negligible to I_C

$$I_{CC} = I_{C1} \cong I_{E1} \cong I_{E2}$$

$$V_O = V_{CC} - I_{CC} R_C$$

If at least one input less than $V_{BE}(FA)$, then the corresponding Q is off. i.e. $I_{CC}=0$

$$V_{OH} = V_{CC}$$

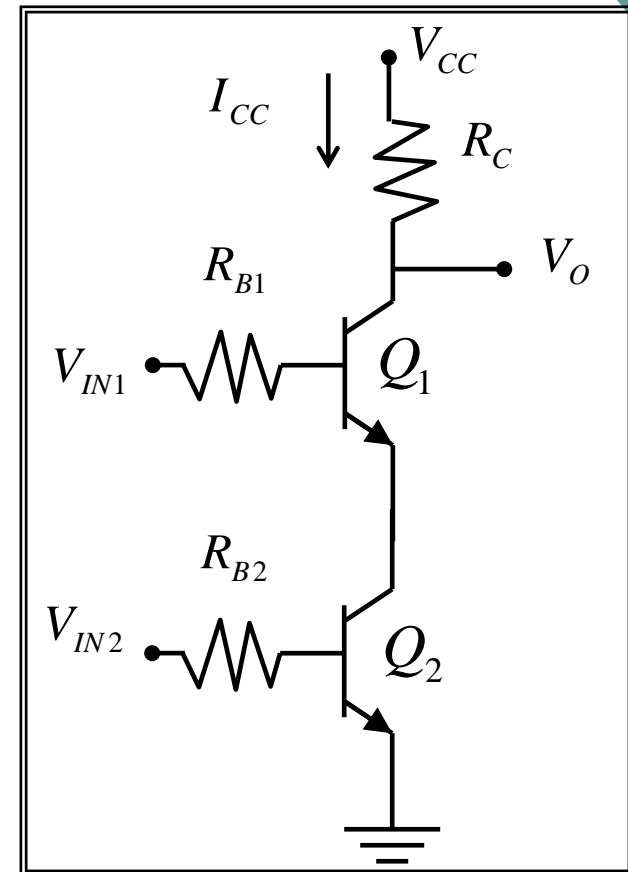
$$V_O = V_{CE}(sat)$$

Q_2 starts conducting (ON) if $V_{IN2} > V_{BE2}(FA)$

Q_1 starts conducting (ON) if $V_{IN1} > V_{BE1}(FA) + V_{CE2}(sat)$

If both Q_1 and Q_2 are saturated

$$V_O = 2V_{CE}(sat)$$



V_O starts decreasing below V_{CC}

Multi-Input RTL NAND Gate

$$V_{OH} = V_{CC} - I_{CC} R_C$$

$$V_{OL} = \sum_{n=1}^N V_{CEn}(sat)$$

Note: Number of inputs of an RTL NAND is limited

Example

Determine the maximum fan-in for basic RTL NAND gate, assuming $V_{CE}(sat) = 0.2V$, $V_{BE}(FA) = 0.7V$

Solution

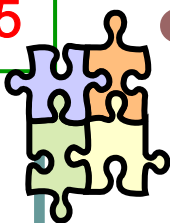
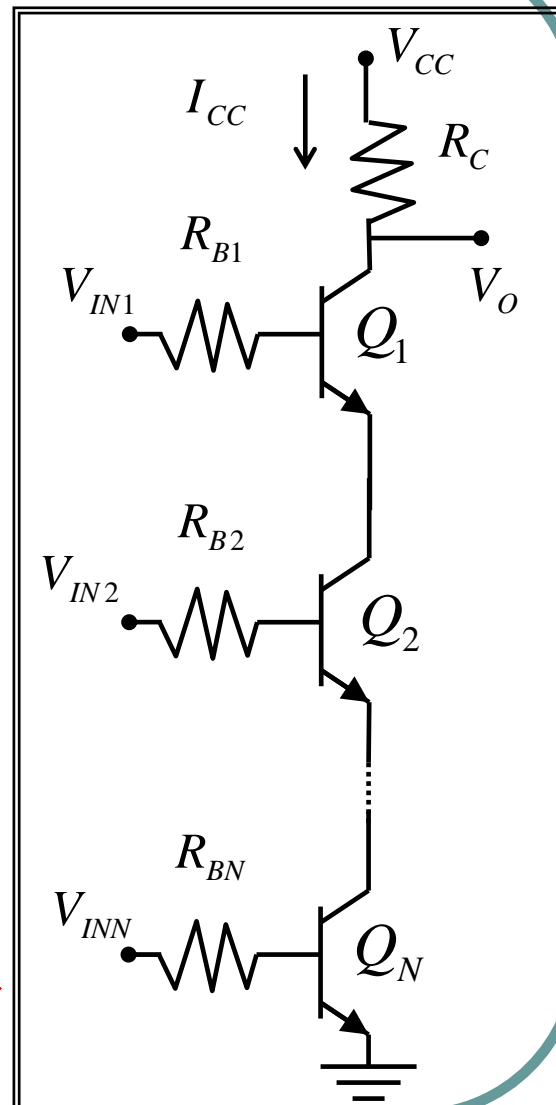
MUST $N_{ML} = V_{IL} - V_{OL} > 0$ $N_{MH} = V_{OH} - V_{IH} > 0$

$$V_{IL} > V_{OL} \Rightarrow 0.7 > N \times V_{CE}(sat) \quad \rightarrow$$

$$N < \frac{0.7}{0.2} = 3.5 \Rightarrow N = 3$$

Always valid

$$V_{OH} > V_{IH} \Rightarrow V_{CC} > V_{BE}(FA) \quad \checkmark$$



RTL Fan-Out

① When an RTL gate is at output **low** state, then any load RTL gate will be in cut-off and draws **no** current

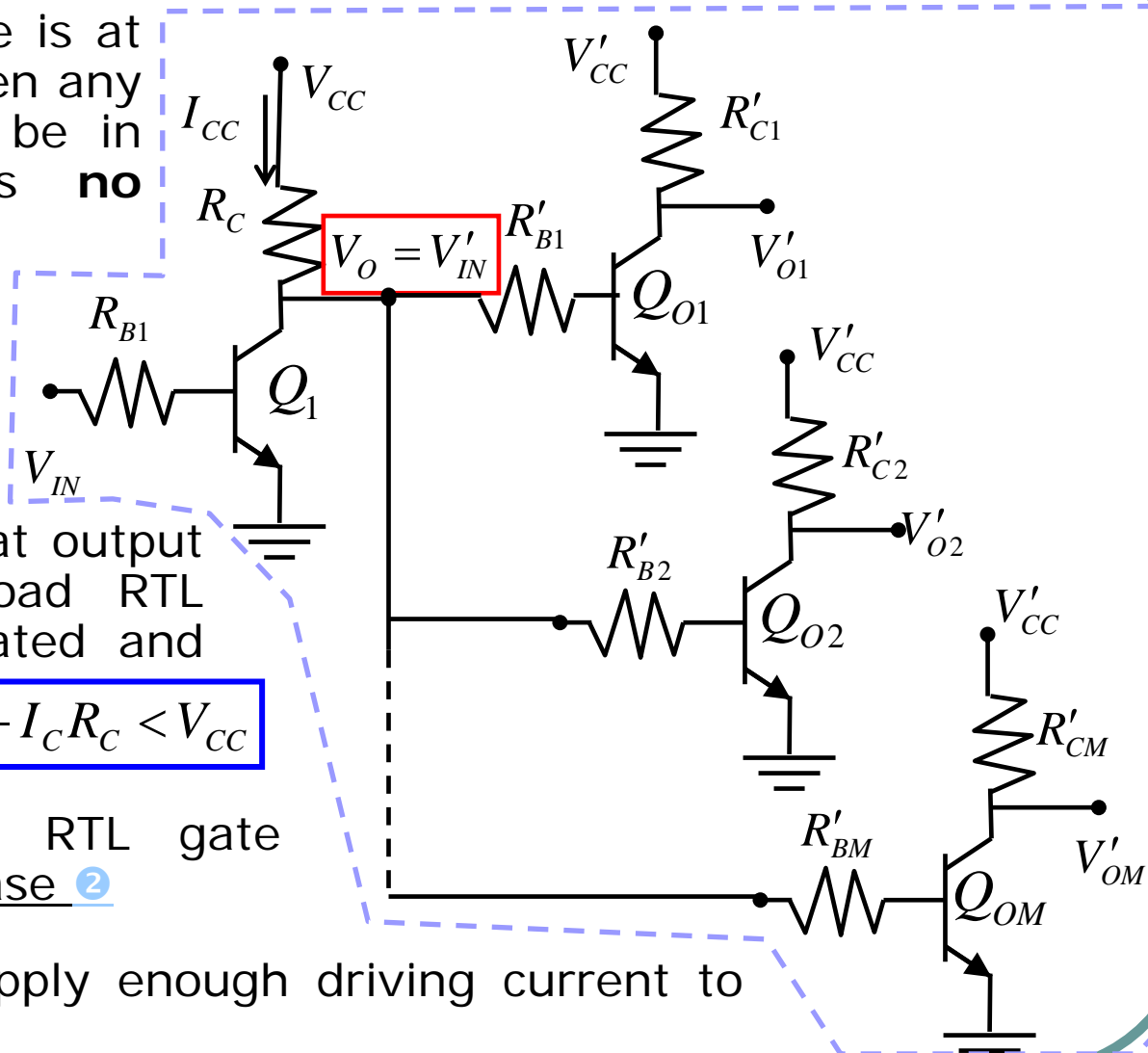
$$V_{OL} = V_{CE}(sat) = V'_{IN} < V_{BE}(FA)$$

② When an RTL gate is at output **high** state, then all load RTL gates will be in saturated and draw current

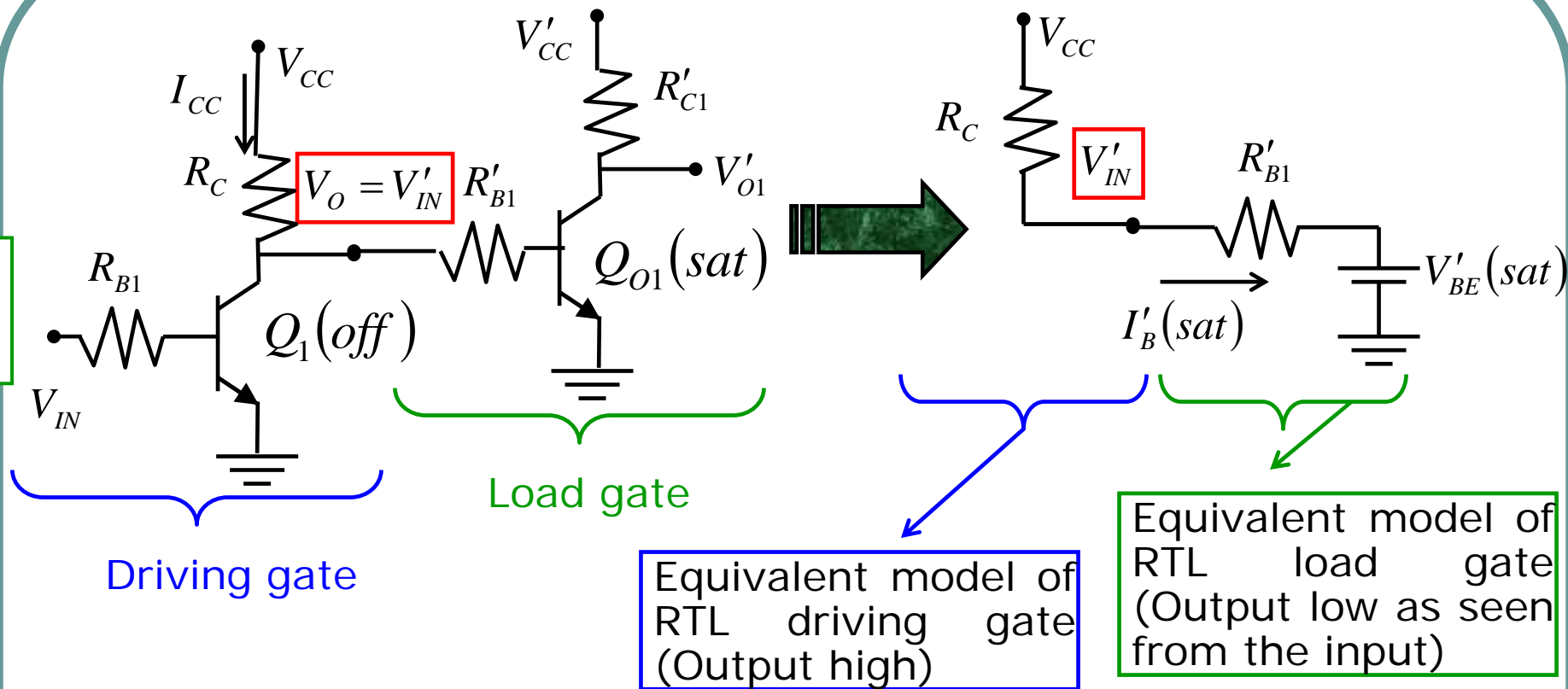
$$V_{OH} = V_{CC} - I_C R_C < V_{CC}$$

③ Maximum fan-out of RTL gate therefore depends on case ②

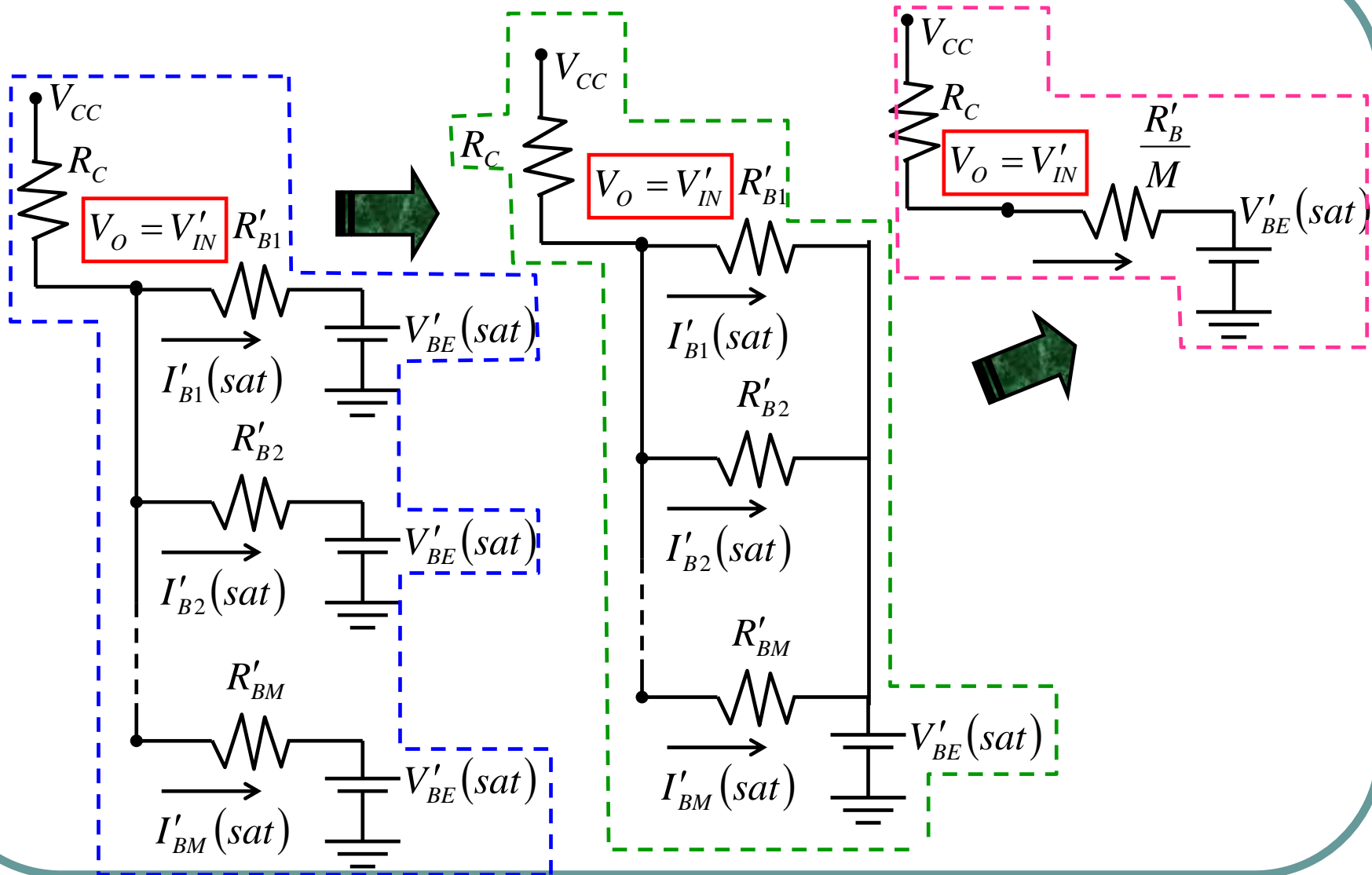
④ Driving gate must supply enough driving current to saturate all load gates



RTL Fan-Out



RTI Fan-Out

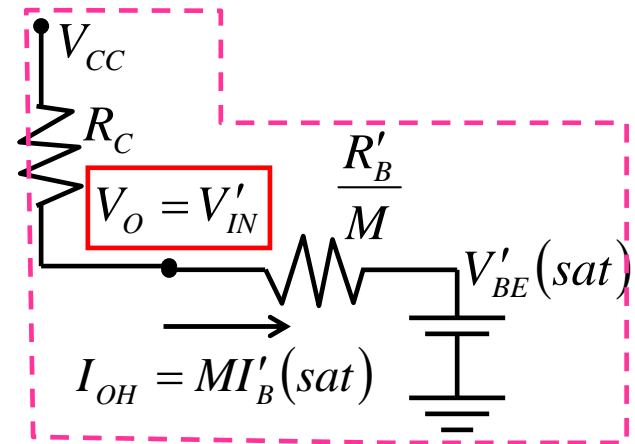


RTL Fan-Out

$$\frac{V_{CC} - V_O}{R_C} = \frac{V_O - V_{BE}(sat)}{R'_B / M}$$

$$M = \frac{(V_{CC} - V_O) / R_C}{(V_O - V_{BE}(sat)) / R'_B} \quad \star$$

$$M = \frac{I_{OH}}{I_{IH}}$$

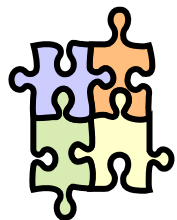


- ① As M increases, the collector current of the driving gate increases, i.e. V_{OH} decreases. V_{OH} should be large enough to saturate all load gates

$$V_{OH}(\min) = V_{IH} = \frac{V_{CC} - V_{CE}(sat)}{\beta_F R'_C} R'_B + V'_{BE}(sat) \quad \star \star \quad (\text{Proved in p. 10 of CH.4})$$

- ② Now, substituting $V_{OH}(\min)$ ($\star \star$) as V_O in (\star) gives the maximum fan-out

RTL Fan-Out



Example

Determine the maximum fan-out for driving RTL gate, assuming

$V_{CE}(\text{sat}) = 0.2\text{V}$,

$V_{BE}(\text{sat}) = 0.8\text{V}$,

$\beta_F = 25$, $V_{CC} = 5\text{V}$,

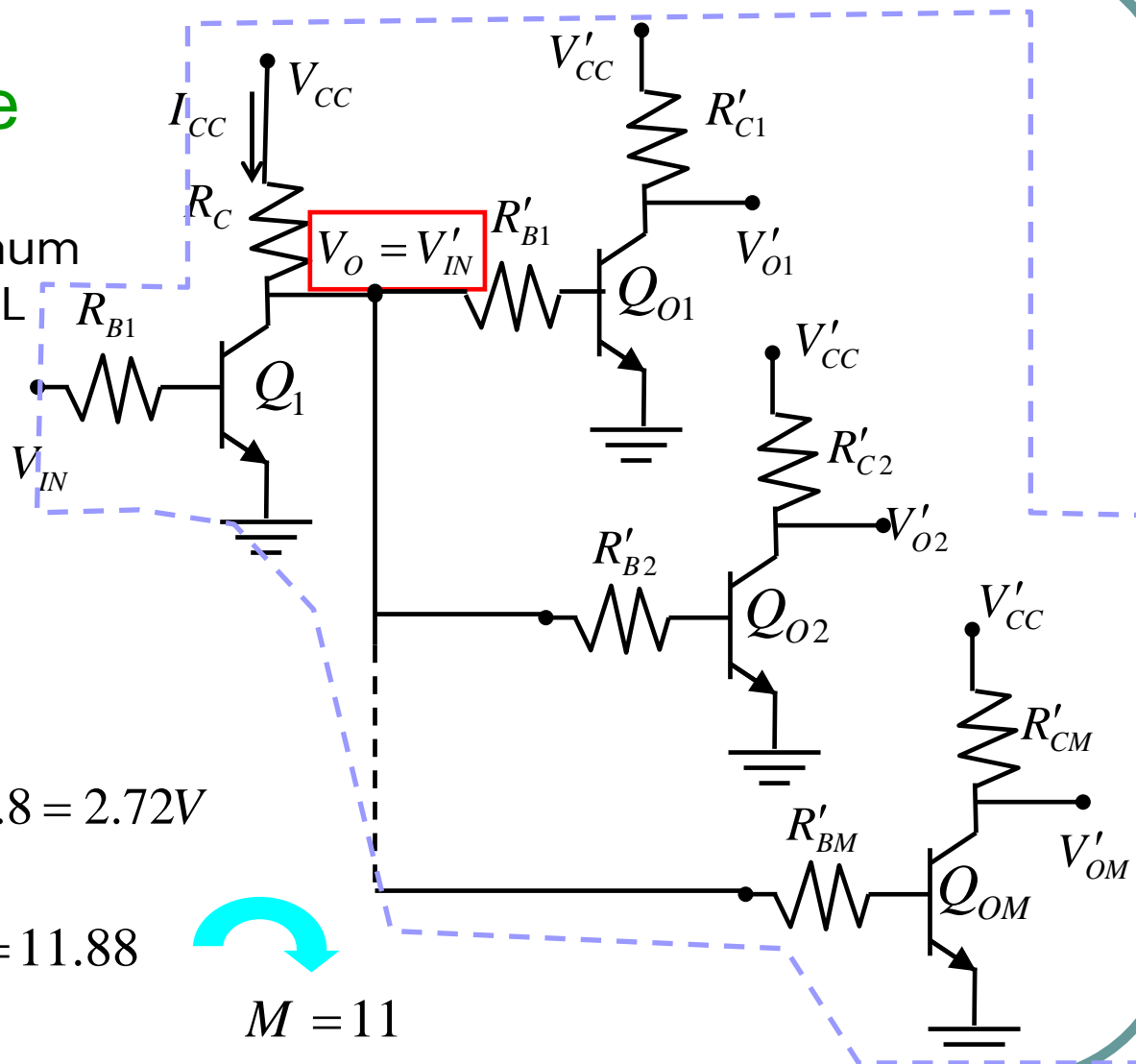
$R_C = 1\text{k}\Omega$, $R_B = 10\text{k}\Omega$

Solution

$$V_{OH}(\text{min}) = \frac{5 - 0.2}{25} \times 10 + 0.8 = 2.72\text{V}$$

$$\text{But } M = \frac{(5 - 2.72)/1}{(2.72 - 0.8)/10} = 11.88$$

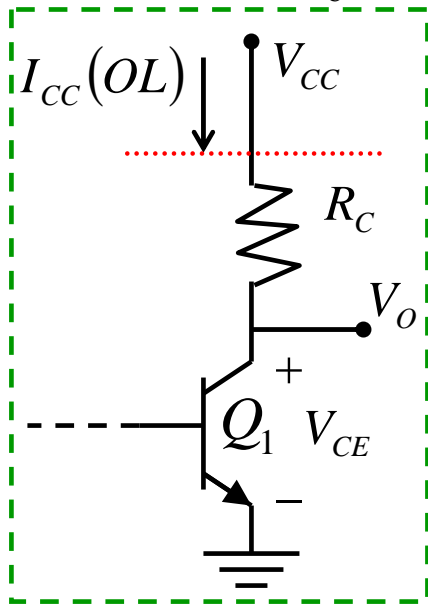
$$M = 11$$



RTL Power-Dissipation

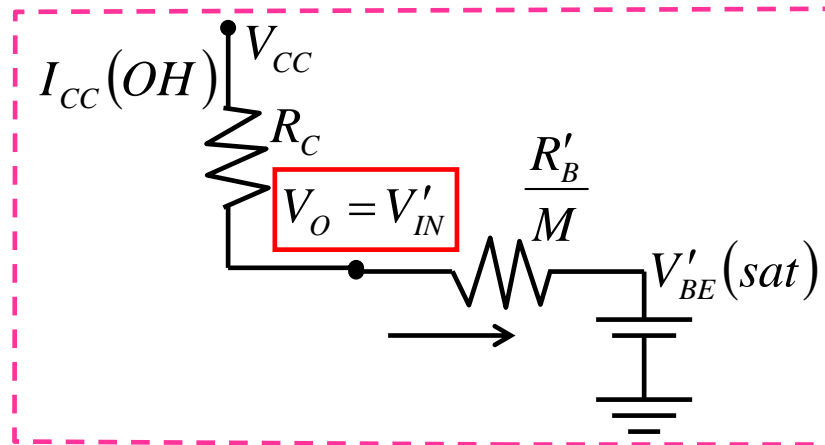
Output low supplied current
 $= I_{CC}(OL)$

$$I_{CC}(OL) = \frac{V_{CC} - V_{CE}(sat)}{R_C}$$



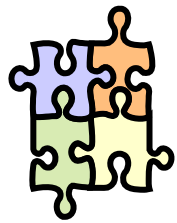
Output high supplied current
 assuming M-load gates
 $= I_{CC}(OH)$

$$I_{CC}(OH) = \frac{V_{CC} - V_{BE}(sat)}{R_C + \frac{R'_B}{M}}$$



$$P_{CC}(avg) = V_{CC} \left(\frac{I_{CC}(OH) + I_{CC}(OL)}{2} \right)$$

RTL Power-Dissipation



● Example

Determine the average dissipated power for

A. No load

B. Fan-out of 1

Assuming $V_{CE}(sat)=0.2V$, $V_{BE}(sat)=0.8V$, $\beta_F=25$, $V_{CC}=5V$,
 $R_C=1k\Omega$, $R_B=10k\Omega$

● Solution

A. No load:

$$I_{CC}(OL) = \frac{V_{CC} - V_{CE}(sat)}{R_C}$$
$$= \frac{5 - 0.2}{1} = 4.8mA$$

$$I_{CC}(OH) = 0mA$$

$$P_{CC}(avg) = 5 \left(\frac{4.8}{2} \right) = 12mW$$

B. $M=1$:

$$I_{CC}(OL) = \frac{V_{CC} - V_{CE}(sat)}{R_C}$$
$$= \frac{5 - 0.2}{1} = 4.8mA$$

$$I_{CC}(OH) = \frac{V_{CC} - V_{BE}(sat)}{R_C + \frac{R'_B}{M}}$$
$$= \frac{5 - 0.8}{1 + 10} = 0.382mA$$

$$P_{CC}(avg) = 5 \left(\frac{4.8 + 0.382}{2} \right)$$
$$= 12.96mW$$

Basic RTL Non-Inverter (Emitter Follower in

● Voltage-Transfer Characteristics

For $V_I - GND < V_{BE}(FA) \rightarrow$

$$I_B = 0, I_C = 0, V_O = 0 = V_{OL}$$

For $V_I - GND \geq V_{BE}(FA) \rightarrow$

$$I_B = (V_I - V_{BE}(FA)) / (R_B + (1 + \beta_F) R_E),$$

$$V_O = R_E (V_I - V_{BE}(FA)) / (R_B / (1 + \beta_F) + R_E)$$

For $V_I - GND \geq V_{IH} \rightarrow$

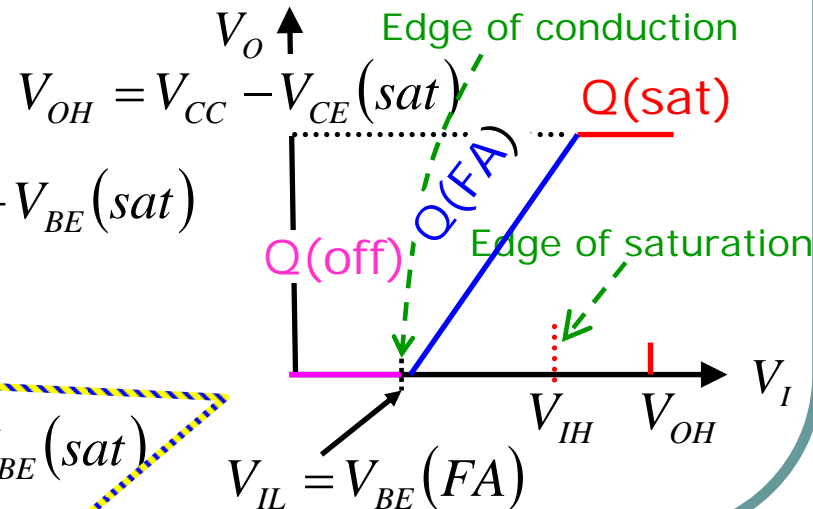
$$I_E = (V_{CC} - V_{CE}(sat)) / R_E$$

$$V_O = V_{CC} - V_{CE}(sat) = V_{OH}$$

$$V_{IH} = I_B(sat) R_B + V_{BE}(sat)$$

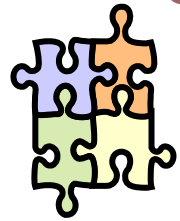
$$+ I_E(sat) R_E$$

$$= I_E(EOS) \left(R_E + \frac{R_B}{(1 + \beta_F)} \right) + V_{BE}(sat)$$



$$V_{IH} = \frac{V_{CC} - V_{CE}(sat)}{R_E} \left(R_E + \frac{R_B}{(1 + \beta_F)} \right) + V_{BE}(sat)$$

BJT Non-Inverter (Basic RTL Non-Inverter)



● Example

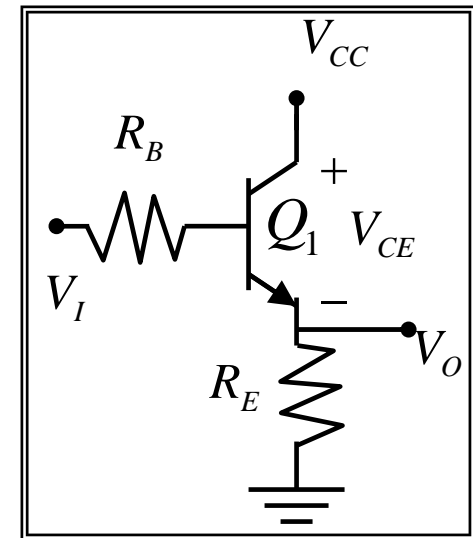
Assume $V_{CC} = 5\text{ V}$, $R_E = 1\text{ k}\Omega$, $R_B = 10\text{ k}\Omega$, $\beta_F = 25$;
 $V_{CE}(\text{sat}) = 0.2\text{ V}$, $V_{BE}(\text{sat}) = 0.8\text{ V}$, $V_{BE}(\text{FA}) = 0.7\text{ V}$,

Determine the VTC parameters

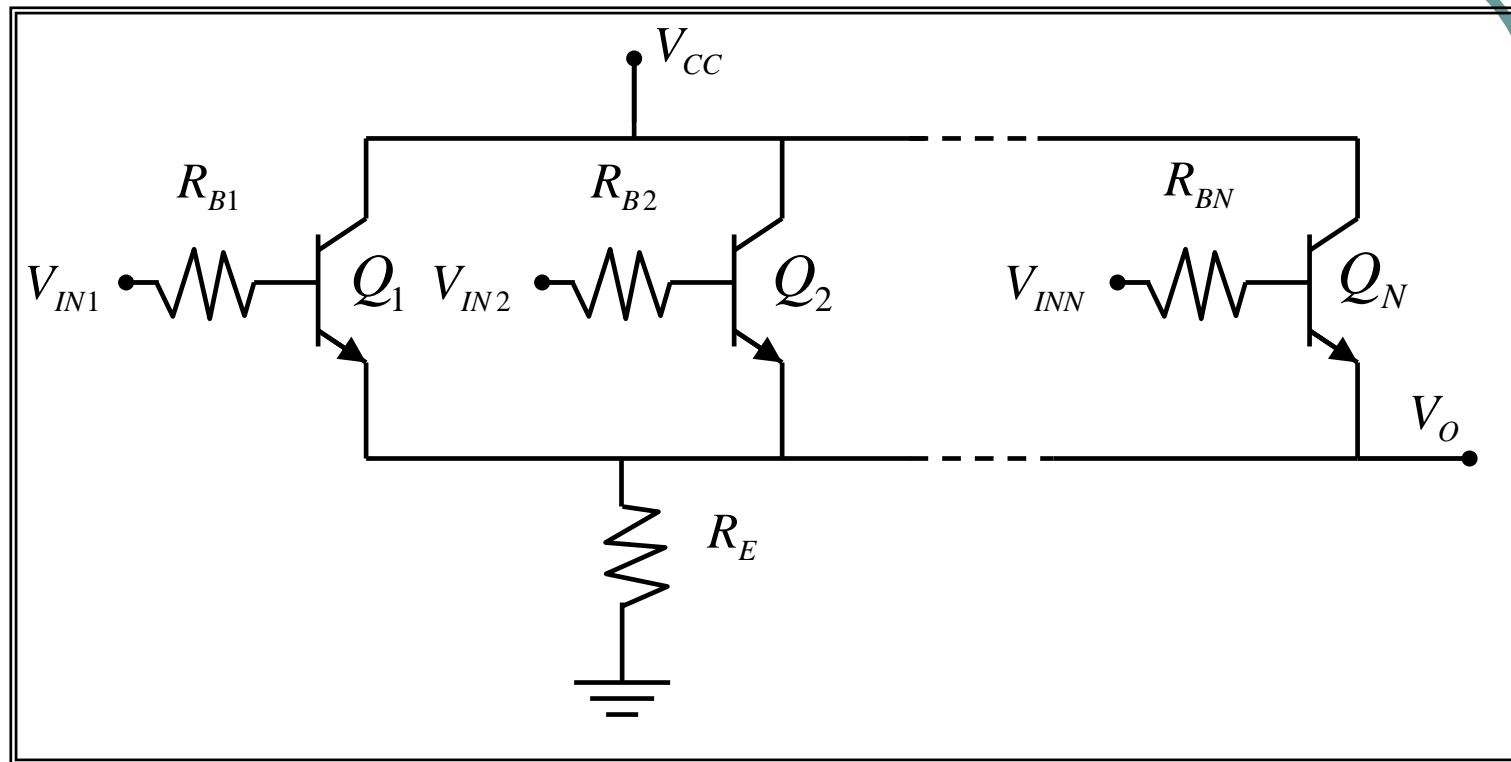
● Solution

$$\begin{aligned} V_{IL} &= 0.7\text{ V}, \\ V_{OL} &= 0.0\text{ V}, \end{aligned}$$

$$\begin{aligned} V_{IH} &= 7.45\text{ V}, \\ V_{OH} &= 4.8\text{ V}, \end{aligned}$$



Basic RTL OR Gate



If all inputs are less than $V_{BE}(FA)$ $\Rightarrow V_O = 0$ Low

If at least one input is greater than V_{IH} $\Rightarrow V_O = V_{CC} - V_{CE}(sat)$ High